

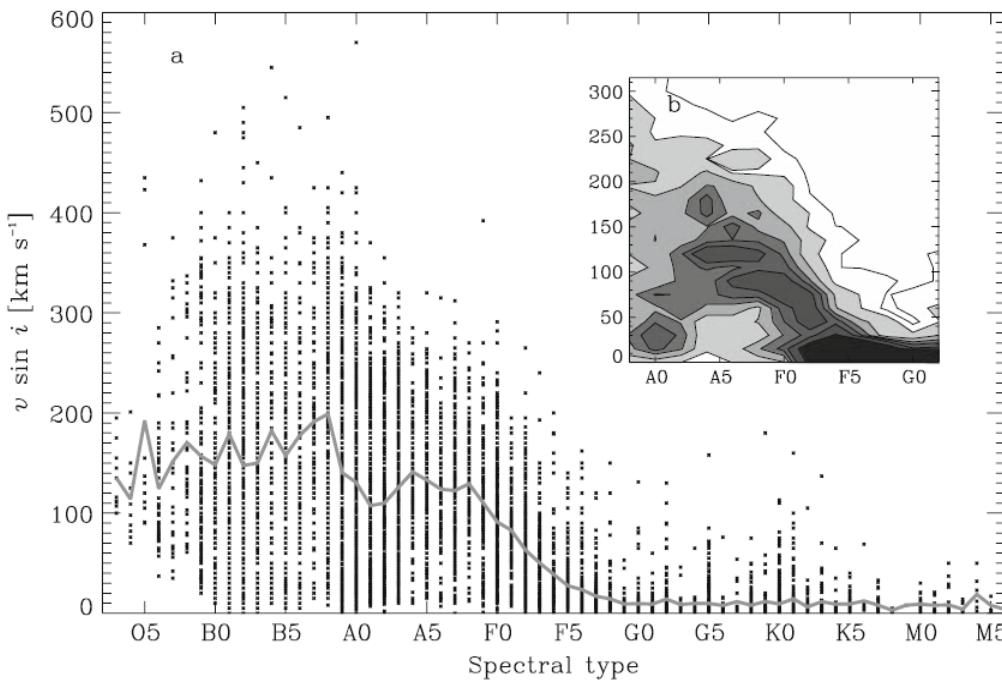
Seismology of rapidly rotating stars

**Jérôme Ballot
F. Lignières,
V. Prat,
D. R. Reese,
M. Rieutord,
G. Mirouh**

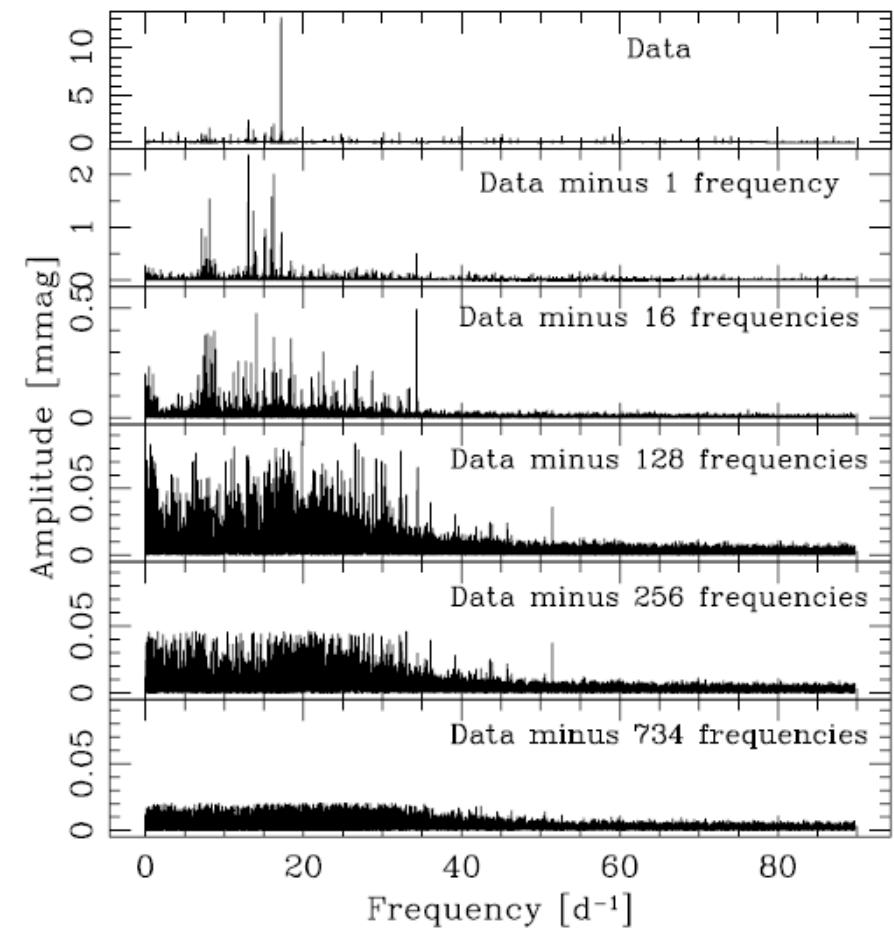
Prospective PNPS - Besançon - 25.02.2014

Rapid rotation

- High rotation is common in intermediate- and high-mass stars
 - ◆ δ Scuti, γ Dor, SPB...
- Complicated spectra



Royer (2009)



Garcia-Hernandez et al 2012

δ Scuti

What is a “rapid rotation”?

➤ Perturbative developments

$$\omega_{nlm} = \omega_{nl0} + C_{nlm}^1 \Omega + C_{nlm}^2 \Omega^2 + C_{nlm}^3 \Omega^3$$

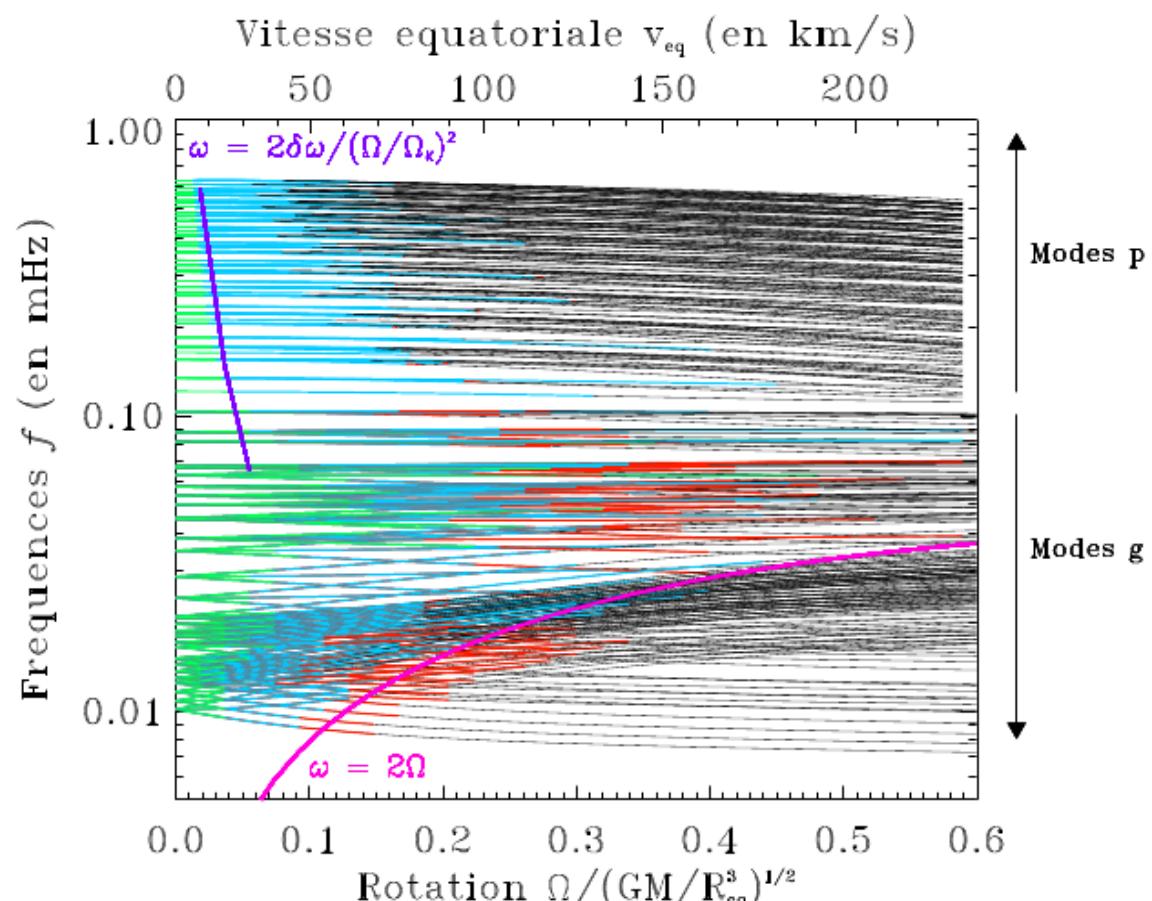
- ◆ Valid as long as $\Omega \ll \omega$ and $\Omega \ll \Omega_K$

Coriolis force

Centrifugal force

What does “negligeable”
mean in practice?

Reese et al. 2006
Ballot et al. 2010
Ballot, Lignières, Reese 2013



Computing oscillation modes

➤ Governing Equations

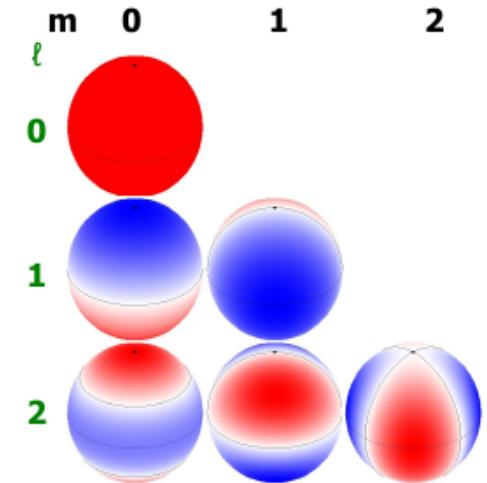
$$\begin{aligned}\partial_t \rho + \nabla \cdot (\rho_0 \mathbf{u}) &= 0, \\ \rho_0 \partial_t \mathbf{u} + 2\rho_0 \Omega \wedge \mathbf{u} &= -\nabla P + \rho \mathbf{g}_0 - \rho_0 \nabla \psi, \\ \partial_t P + \mathbf{u} \cdot \nabla P_0 &= c_s^2 (\partial_t \rho + \mathbf{u} \cdot \nabla \rho_0), \\ \Delta \psi &= 4\pi G \rho,\end{aligned}$$

➤ $\Omega=0 \rightarrow$ spherical symmetry

- ◆ Solutions in the form $g(\vec{x}) = f(r) \underbrace{P_\ell^m(\theta) \exp(im\phi)}_{Y_{\ell m}}$
- ◆ \rightarrow 1D eigenvalue problem

➤ $\Omega \neq 0 \rightarrow$ axial and equatorial symmetry

- ◆ Solutions in the form $g(\vec{x}) = f(\vec{x}_M) \exp(im\phi)$
- ◆ \rightarrow 2D eigenvalue problem (2D models needed!)
- ◆ \rightarrow to be solved with the TOP code (Reese et al 2006)
ACOR code (Ouazzani 2012)



2D models are needed

➤ Computation from 1-D structure models

- ◆ No distortion / 2nd order perturbation

➤ Polytropic 2-D models

- ◆ Intensively used to explore spectra

➤ Realistic 2-D models: ESTER code

[Espinosa Lara & Rieutord 2007, 2012, Rieutord & Espinosa Lara 2009, 2013]

- ◆ 2-D structures of massive stars

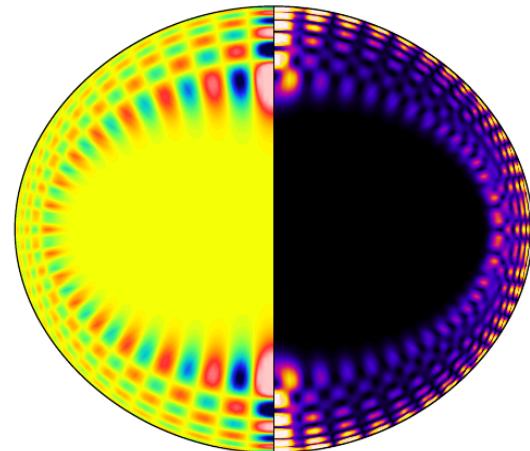
- M, Ω , X_c

- ◆ Code under GPL

- Web: www.ast.obs-mip.fr/users/rieutord/ESTER.html
<http://code.google.com/p/ester-project/>

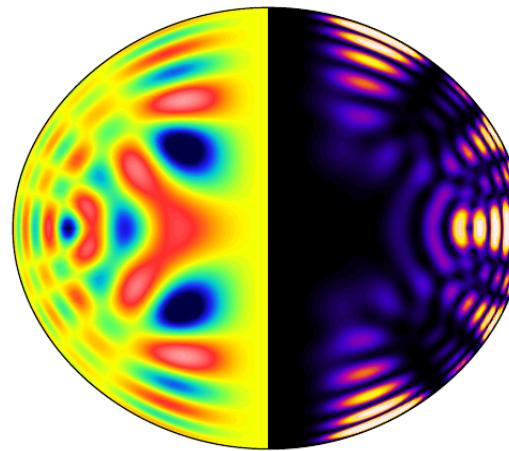
➤ New families of modes (Spectrum = Σ subspectra)

Whispering gallery mode



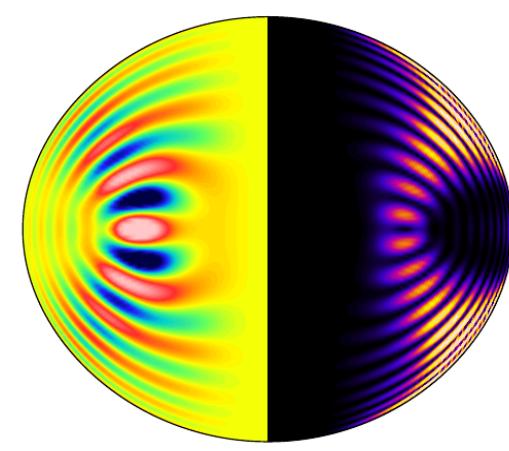
(d)

chaotic mode

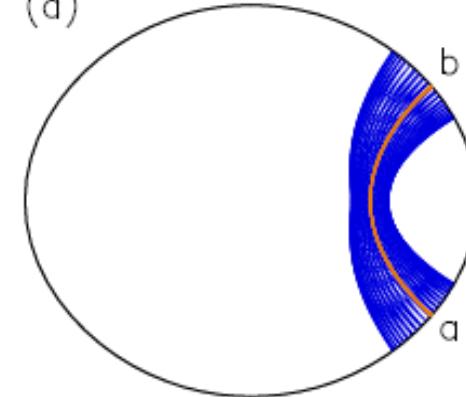
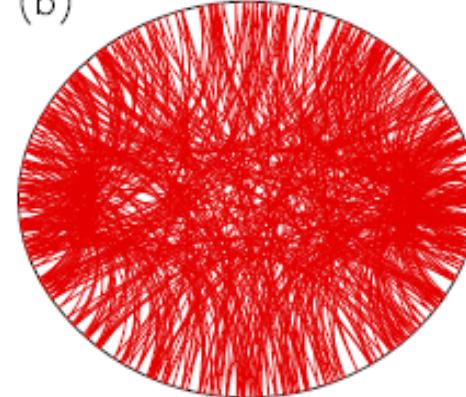
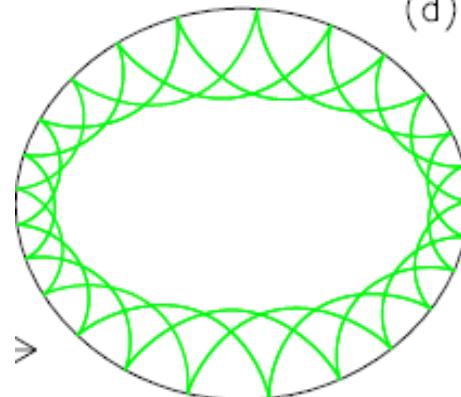


(b)

island mode



(a)



◆ classification with ray theory (Lignières & Georgeot 2008,2009)

p-mode regularities

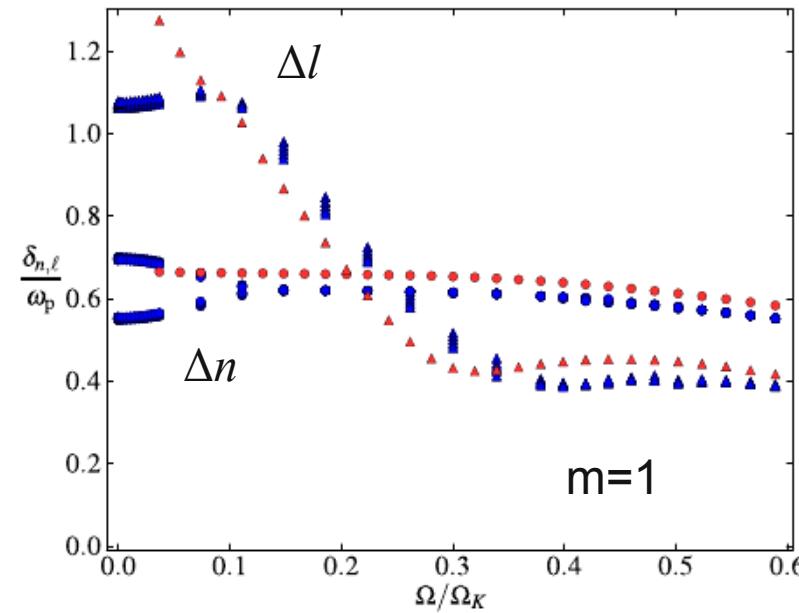
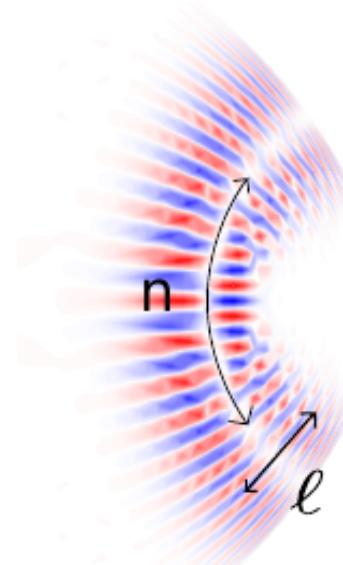
- Regularities derived for non-rotating stars are lost, new regularities (for island modes) emerge

- ◆ Empirical relations (e.g. Lignières et al. 2006, Reese et al. 2006, 2009)

$$\omega_{n,\ell,m} = n\Delta_n + \ell\Delta_\ell + |m|\Delta_m + \alpha^\pm$$

- ◆ Asymptotic theory (Pasek et al. 2011, 2012)

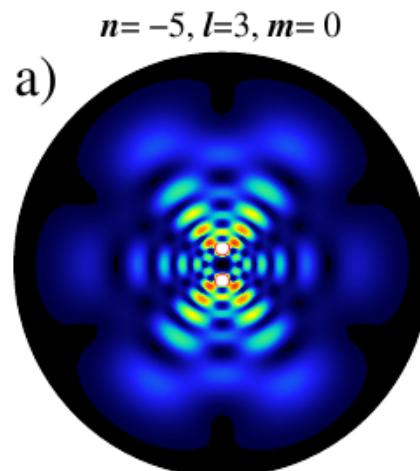
$\Delta \leftrightarrow$ structure



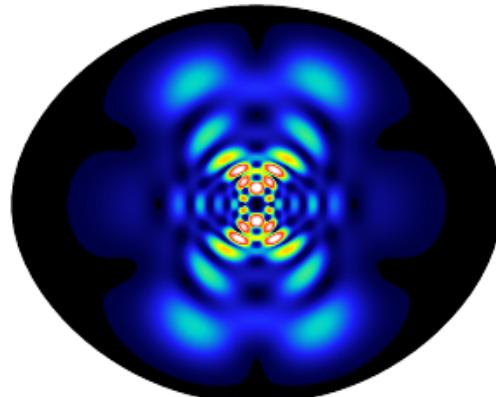
g modes in rotating stars

➤ Different behaviours

$\Omega=0$



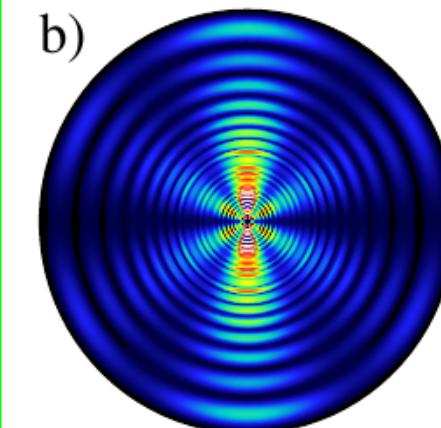
$\Omega=0.7\Omega_K$



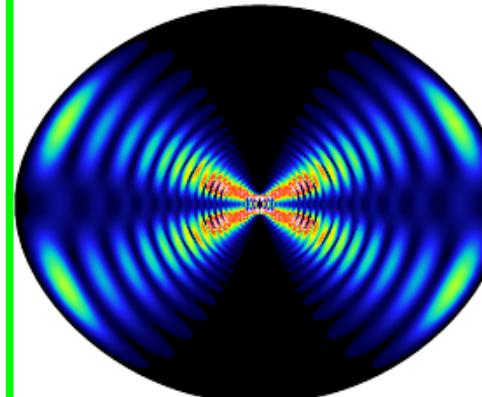
$\omega > 2\Omega$

$\omega < 2\Omega$

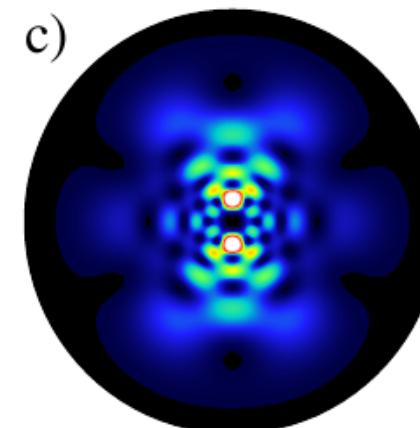
b) $n = -20, l = 3, m = -1$



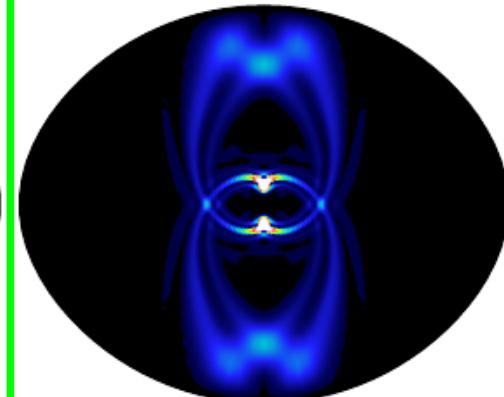
critical latitude
(cf DIntrans 2000)



c) $n = -3, l = 3, m = 0$



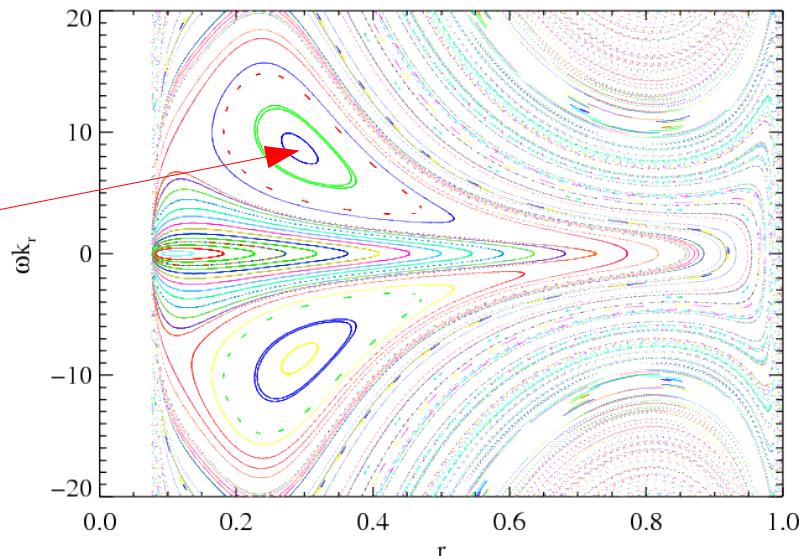
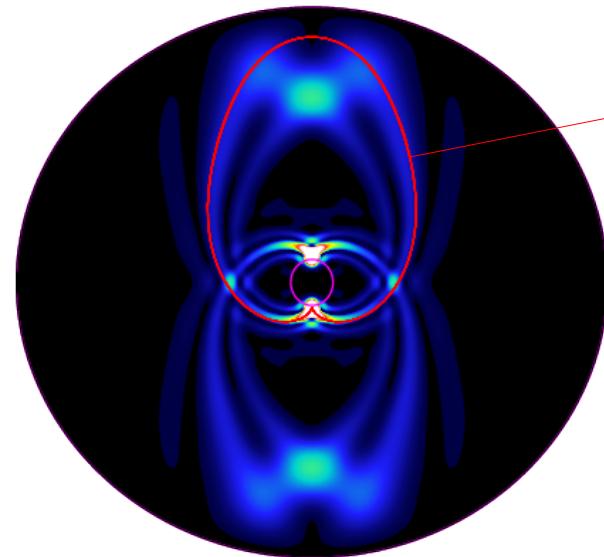
rosette mode
(Ballot et al. 2012)



$\omega > 2\Omega$

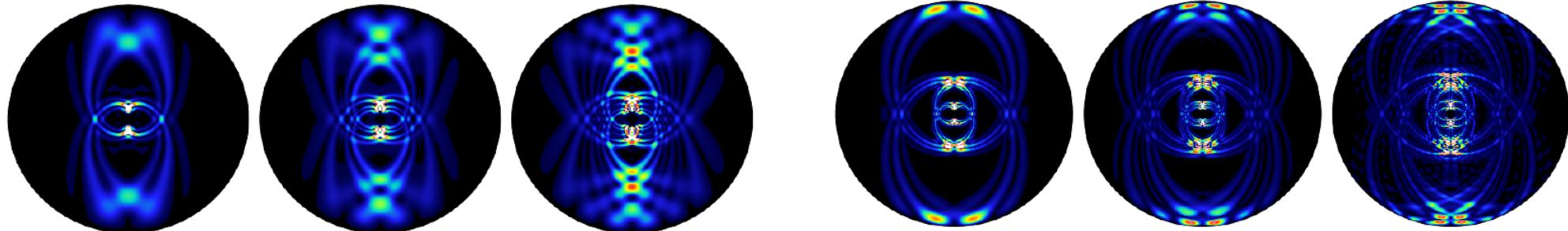
Rosette modes

- Rosette modes are associated with stable trajectories



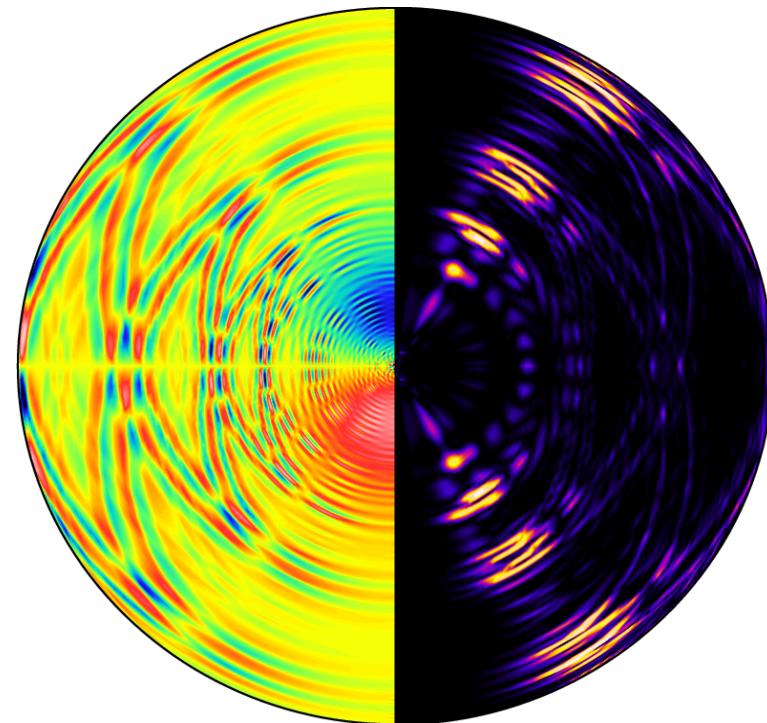
Ballot et al. 2012

- Several families of rosette modes

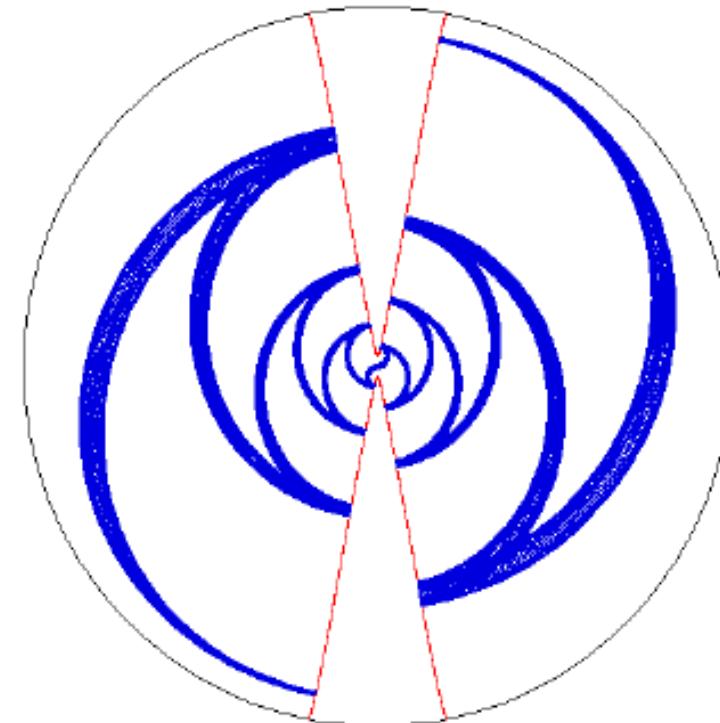


Bat-modes

- Modes in the inertial domain also associated to stable trajectories



Ballot et al., en prep.



Prat 2010

Regularities of g modes: period spacings

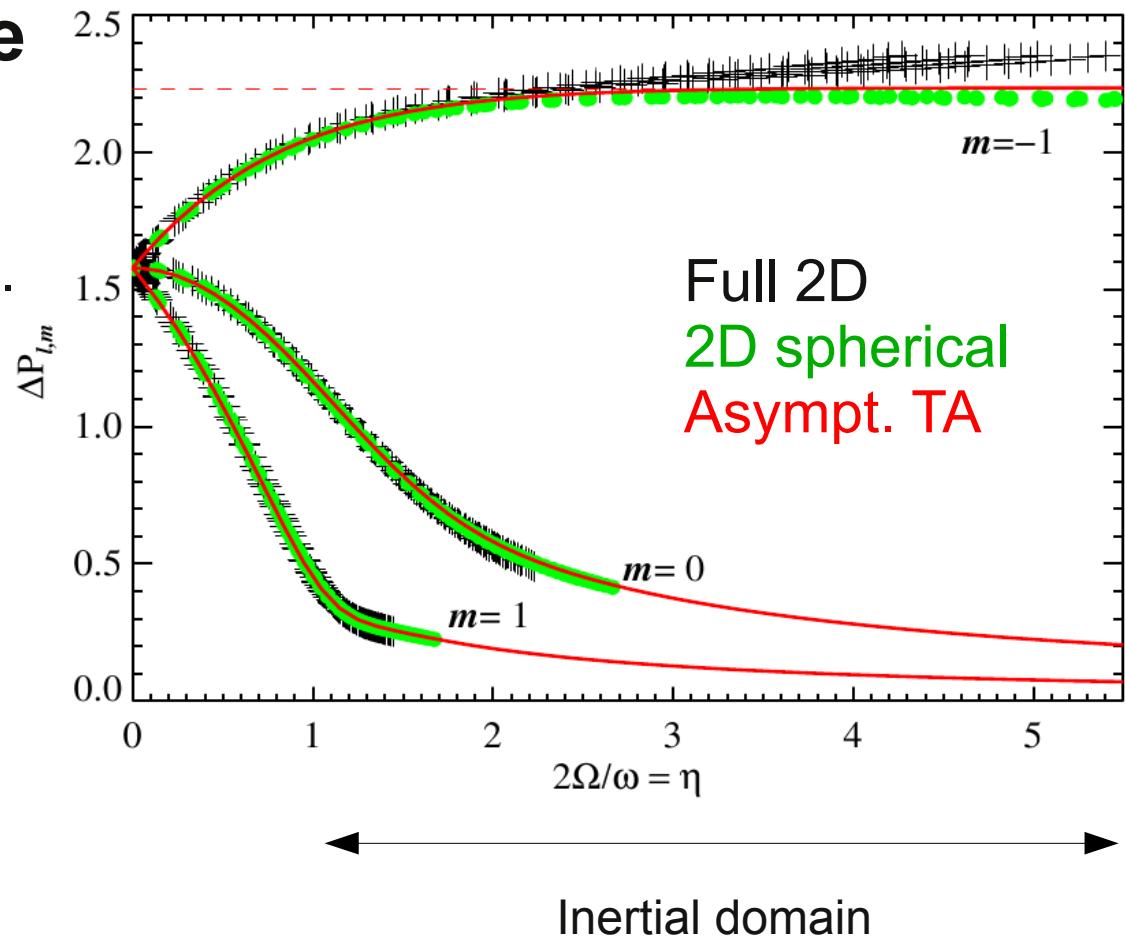
➤ ΔP as a function of $\eta = 2\Omega P = 2\Omega/\omega$

➤ Spacings compatible with the Traditional approximation

[Eckart 1960, Berthomieu et al. 1978, Lee & Saio 1987]

➤ However

- ◆ T.A. cannot predict rosette/bat modes
- ◆ T.A.: problem with convective core

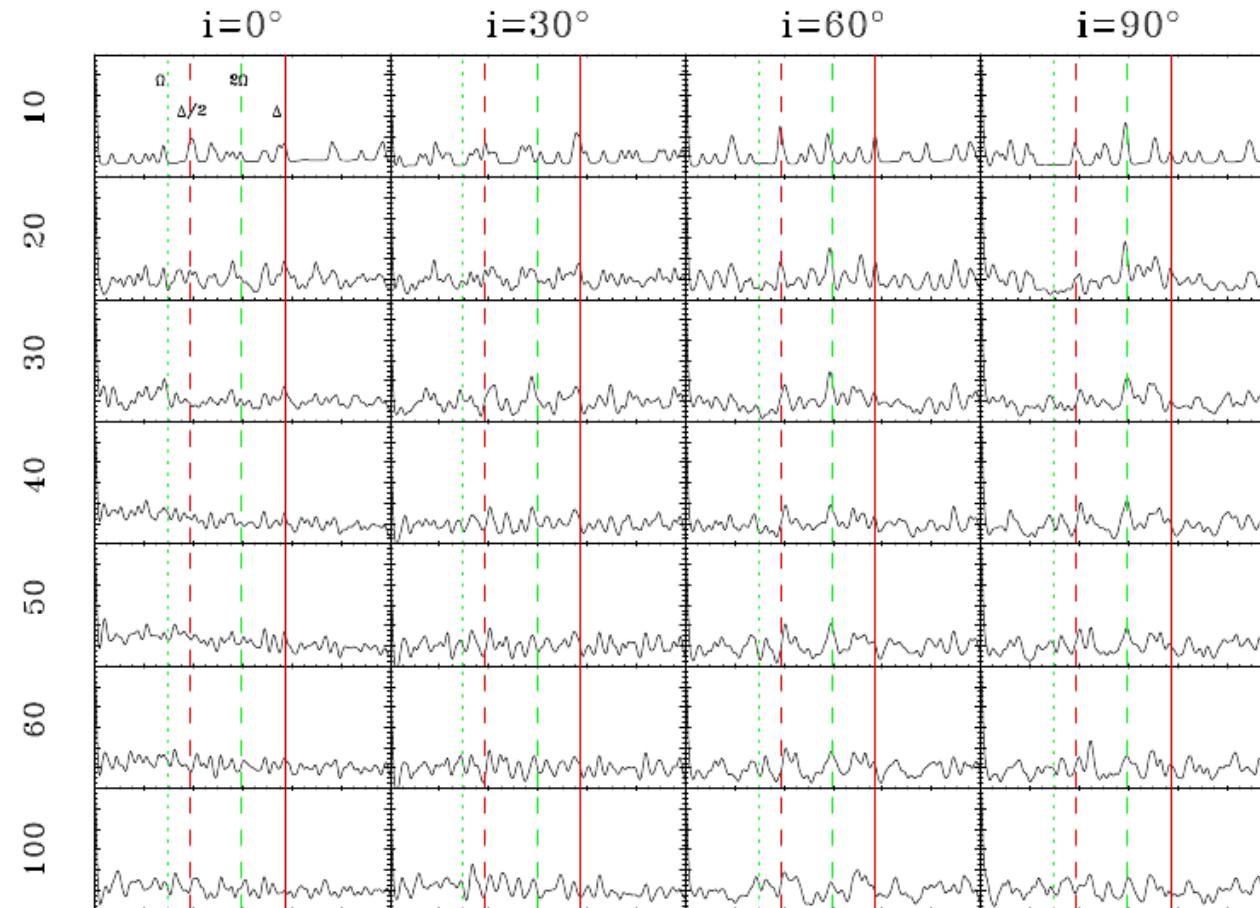


[Ballot et al. 2012]

Comparison with observations

➤ Looking for regularities

- ◆ AC, PSPS according to the configuration contraction of Δ or $\Delta/2$, sometimes 2Ω



Direct comparison

➤ 2D model of α Oph w. ESTER

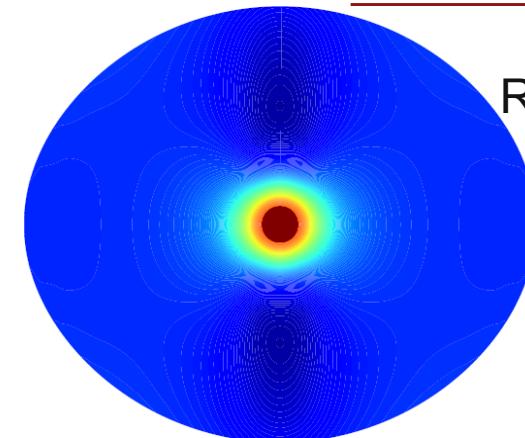
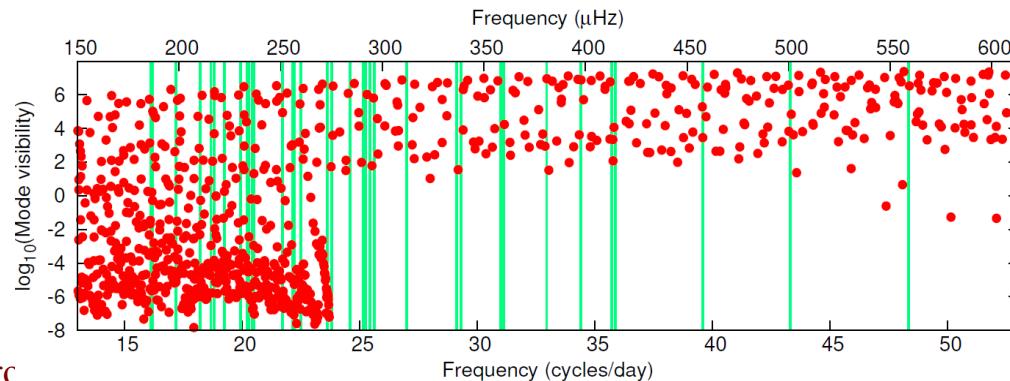
- ◆ Observational constraints
 - Interferometry (Zhao et al. 2009)

➤ Oscillations w. TOP

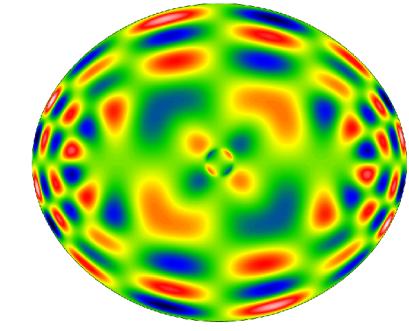
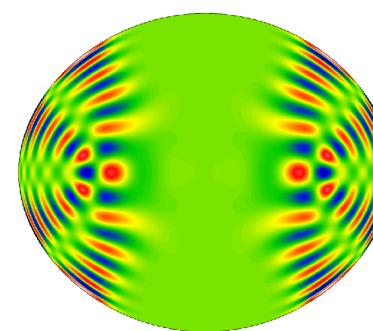
- ◆ Modes+visib.+damping
- ◆ Observations

(Monnier et al 2010)

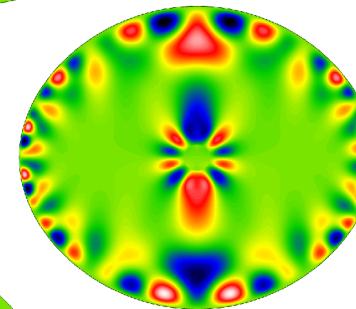
Mirouh et al. 2013



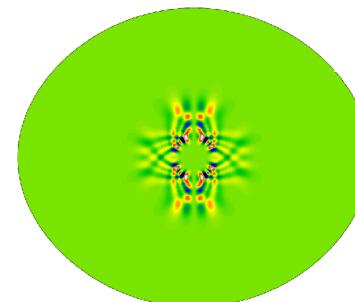
Rotation



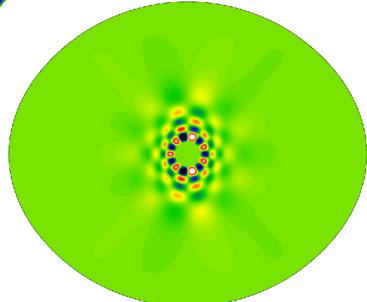
p



p-g



g



➤ **Better understanding of p- and g-mode spectra**

- ◆ mode classification
- ◆ regularities

➤ **Data exploitation**

- ◆ Looking for regularities in spectra
 - simple to implement. Interpretation?
- ◆ Direct comparison
 - time consuming. work in progress
- ◆ Issue: predicting mode amplitudes



The Space Photometry Revolution

CoRoT Symposium 3, Kepler KASC-7 joint meeting

6-11 Jul 2014 Toulouse (France)

6-11 Jul 2014, Toulouse

<http://corot3-kasc7.sciencesconf.org/>

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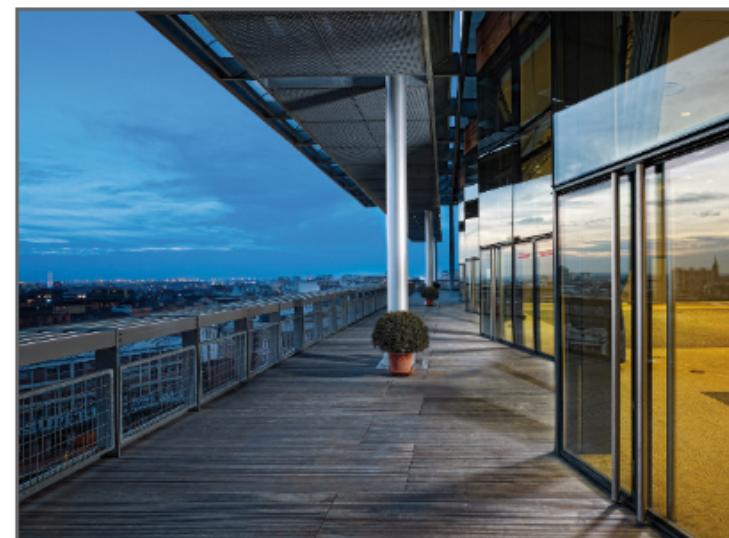
FINANCIAL SUPPORT

VENUE

The conference will be held at **Espaces Vanel, Toulouse (France)**.

Situated in the South-West of France, close to the Pyrénées mountains, Toulouse is a friendly and attractive town benefiting from the sunny and mild weather of southern France. It can be easily reached by plane through Toulouse-Blagnac international airport (<http://www.toulouse.aeroport.fr>) located at 10 km from Toulouse city centre.

The access to the Espaces Vanel is easy. It is located in downtown Toulouse, a 5-minute walk away from the central train station (Toulouse Matabiau) and a 10-minute walk away from the historic centre.



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